

## Homework

due on Friday, February 18

Read carefully sections 4.2-4.5 in the book. Solve the following problems.

**Problem 1.** Write the row of Pascal triangle which corresponds to  $n = 7$  Prove by induction that  $7|n^7 - n$  for every natural number  $n$ . Conclude that the same is true for every integer  $n$ .

**Problem 2.** The sequence  $x_n$  is defined recursively as follows:

$$x_0 = 0, \ x_1 = 2, \ x_{n+1} = 2x_n - x_{n-1} + 2.$$

Prove by induction that  $x_n = n^2 + n$ .