Challenging Problems for Math 523

Problem 1. Let r, s, t be integers greater than 1. Prove that there exists a finite group G which contains elements a, b of orders r, s respectively such that ab has order t.