

Math 148 Quiz Five Version A

Name:

1. Answer the following questions:

(a) What does it mean for two events to be mutually exclusive?

Two events are mutually exclusive if they cannot happen at the same time. $P(A \text{ and } B) = 0$

(b) What does it mean for two events to be independent?

The occurrence of one event has no effect on the possibility of the occurrence of the other. $P(A|B) = P(A)$ and $P(B|A) = P(B)$

2. A deck of cards is shuffled and a card is drawn. Let A be the event that the card is a club and B be the event that the card is a king.

(a) Calculate the following probabilities: $P(A)$, $P(B)$, $P(A \text{ and } B)$, $P(A \text{ or } B)$, $P(A \text{ given } B)$, $P(B \text{ given } A)$.

$$\begin{aligned}P(A) &= 13/52 = 1/4 & P(B) &= 4/52 = 1/13 & P(A \text{ and } B) &= 1/52 \\P(A \text{ or } B) &= 13/52 + 4/52 - 1/52 = 16/52 = 4/13 \\P(A|B) &= 1/13 & P(B|A) &= 1/4\end{aligned}$$

(b) Are the events A and B independent? Explain.

Yes because $P(A|B) = P(A)$ and $P(B|A) = P(B)$

(c) Are the events A and B mutually exclusive? Explain.

No, $P(A \text{ and } B) = 1/52$.