

Math 148 Quiz Seven Version C

Name:

Answer the following questions:

- (4 points) A box contains numbered tickets.
 - Draws are made at random with replacement from the box.
 - For a certain number n of draws, the expected value of the sum S_n of those n draws is $E(S_n) = 300$.
 - For that same number of draws, there is a 75% chance that the sum of the draws S_n is between 250 and 350.

Is the following statement true or false? Explain briefly your response.

There is about a 75% chance that the sum S_{2n} of twice as many draws is between 500 and 700.

False. The EV for S_{2n} increases to 600, but the SE increases to $\sqrt{2}$ SE. Therefore, the 75% confidence interval should be shorter than (500,700)

- (8 points) 400 draws are made at random with replacement from the box $\vec{b} = [1, 3, 5, 7, 9]$.

- Estimate the probability that the sum of the draws S_{400} will be more than 1,500.
- Estimate the probability that the number 3 will be drawn fewer than 90 times.

(a) $EV = 400 \times 5 = 2000$

$SE = \sqrt{400} \times SD = 56.57$

$SU = \frac{1500 - 2000}{56.57} = -8.83$

The probability is approximately 100%

(b) $EV = 400/6 = 66.67$

$SE = \sqrt{400} \times \sqrt{1/6 \times 5/6} = 7.45$

$SU = \frac{90 - 66.67}{7.45} = 3.13$

The probability is approximately 0.08%

- (3 points) A pair of fair dice is tossed once. A correct box model for the sum of the dots is

- The sum of two draws with replacement from the box $[1, 2, 3, 4, 5, 6]$
- One draw from the box $[2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12]$.

Only one of the above is true. Select the correct statement, and explain your reasoning.

(a) is true. The probability that the sum is 2 is $1/36$ and the probability that the sum is 3 is $2/36$, but in (b) they are equal $1/11$.

Thus, it cannot be (b).