

## Math 330 Section 2 - Spring 2017 - Homework 12

*Published: Saturday, March 18, 2017*

*Running total: 46 points*

*Last submission: Extended to Monday, April 3, 2017*

*Updated on Monday, 2017-03-27 with new hints for #1!*

### Status - Reading Assignments:

Here is the status of the reading assignments you were asked to complete by this date.

B/G (Beck/Geoghegan) Textbook:

- all of ch.1 - ch.12 (ch.7 carefully until before thm.7.17, ch.11 until cor.11.23)

MF lecture notes:

- ch.1 - ch.2, ch.4 - ch.6
- all of ch.8.1
- ch.16 (addenda to B/G text)

Other material:

- B/K lecture notes ch.1 – section 1, ch.4.1, ch.4.2  
(optional reading – good for examples, improved understanding)
- Stewart Calculus: “The Precise Definition of a Limit” (ch.1.7 in the 7th edition).

### New reading assignments:

Due to the loss of two lectures because of the snow storm most of the reading for this week is repetition of previous assignments.

#### Reading assignment 1 - due Monday, March 20:

- a. Reread B/G ch.10. I will skip in lecture most of ch.10.1 and 10.2.

Be sure to learn by heart the definition of convergence of a sequence of real numbers and the important laws and formulas on that subject.

#### Reading assignment 2 - due Tuesday, March 21:

- a. Reread MF ch.8 until before def.8.10 (Tail sets of a sequence).

Again, be sure to learn by heart the definition of convergence of a sequence of real numbers and the important laws and formulas on that subject.

#### Reading assignment 3 - due Wednesday, March 22:

- a. Important for those who did not/are not currently taken a linear algebra class: Read carefully MF ch.9.1 ( $\mathbb{R}^N$  : Euclidean Space) and ch.9.2.1 (Vector spaces: Definition and Examples).

#### Reading assignment 4 - due: Friday, March 24:

- a. Read carefully MF ch. 8.2 and the addenda to ch.8 (ver 2017-03-28).

#### Written assignment 1:

Prove B/G prop.10.10(iv):  $x, y \in \mathbb{R} \Rightarrow |x - y| \geq ||x| - |y||$ .

#### Hints:

- a. Use the triangle inequality on  $|x| = |(x - y) + y|$  and then again on  $|y| = |(y - x) + x|$ . See what you get for  $|x| - |y|$  and for  $|x - y|$ .
- b. Examine separately the cases  $|x| \geq |y|$  and  $|x| < |y|$ . It's easy now!

**Written assignment 2:**

Prove B/G prop.10.21(ii):

Let  $\lim_{k \rightarrow \infty} x_k = L$ . If  $(x_k)_{k=0}^{\infty}$  is decreasing then  $x_k \geq L$  for all  $k \geq 0$ .

**Hint:**

- Inspect carefully the proof of B/G prop.10.19: increasing bounded sequence converges. It gives you the argument for increasing sequences.

**Written assignment 3:**

Prove MF prop.8.6.a: Let  $\alpha \in \mathbb{R}$  and  $x_n = \alpha$  for all  $n \in \mathbb{N}$ . Then  $\lim_{k \rightarrow \infty} x_k = \alpha$ .

Prove this using the formal  $\varepsilon$ - $N$  definition of the limit of a sequence (B/G def. at the beginning of ch.10.4 or MF def.8.9)