# Math 330 Section 5 - Fall 2022 - Homework 03

Published: Tuesday, August 30, 2022 Last submission: Wednesday, September 14, 2022

Running total: 16 points

# **Status - Reading Assignments:**

Here is the status of the reading assignments you were asked to complete by this date.

# MF lecture notes:

ch.2.1 – 2.4, ch.3.1 – 3.4 until Def.3.12 (Absolute value).

B/G (Beck/Geoghegan) Textbook: ch.1 – 2.2

B/K lecture notes:

ch.1.1 (Introduction to sets) (optional) ch.1.2 (Introduction to Functions) but skip ch.1.2.4: Floor and Ceiling Functions (optional)

# New reading assignments:

# Reading assignment 1 - due Tuesday(!), September 6:

**a.** Read carefully the remainder of MF ch.3.

# Reading assignment 2 - due Wednesday, September 7:

- **a.** Read very carefully B/G ch.3 on logic. It is extremely short and covers about all I'll teach you on the subject with the exception of truth tables (which you already have encountered when we proved that  $A \triangle B$  is associative).
- **b.** Skim MF ch.4.1 4.4, just so you have an idea what's in there. Note that I have marked all of ch.4 as optional, but you will be tested on B/G ch.3!

# Reading assignment 1 - due Friday, September 9:

- **a.** Skim the remainder of MF ch.4. but look a little bit more closely at ch.4.5.4 (Quantifiers and Negation).
- **b.** Carefully read MF ch.5 through ch.5.2.3. You already encountered some of the material on functions in ch.2.3.

# Written assignments are on the next page.

**General note on written assignments:** Unless expressly stated otherwise, to prove a proposition or theorem you are allowed to make use of everything in the book up to but NOT including the specific item you are asked to prove.

#### Written assignment 1:

Let  $(R, \oplus, \odot)$  be an integral domain. Use anything up-to and including MF prop. 3.27 to prove MF prop.3.28: Let  $x \in R$ . If  $x \odot x = x$  then x = 0 or x = 1.

**Hint:** Prove the following: If  $x \odot x = x$  and  $x \neq 0$  then x = 1. Why is that enough?

### Written assignment 2:

Let  $(R, \oplus, \odot, P)$  be an ordered integral domain. Use anything up-to and including MF prop. 3.34 to prove MF prop.3.35: The multiplicative unit 1 of *R* belongs to *P*.

**Hint:** This is an **indirect proof!** Part of it: Show that you cannot have  $\ominus 1 \in P$ . **Why** will this help you?

You are **strongly advised** to study the proof of Proposition 3.33 (newly added to MF version 2021-09-01) very thoroughly before working on this problem.