# Math 330 Section 1 - Fall 2024 - Homework 03

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## **Status - Reading Assignments:**

The reading assignments you were asked to complete before the first one of this HW are:

#### MF lecture notes:

ch.1; ch.2.1 - 2.6, 3.1 - 3.4 until Def.3.13

B/G (Beck/Geoghegan) Textbook: ch.2.1 – 2.2

B/K lecture notes:

- ch.1.1 (Introduction to sets) (optional)
- ch.1.2 (Introduction to Functions) but skip ch.1.2.4: Floor and Ceiling Functions (optional)

## New reading assignments:

## Reading assignment 1 - due Monday, September 2 (Labor Day):

- **a.** Read carefully the remainder of MF ch.3.4. Propositions 3.52 and 3.53 will be seen again when we talk about normed vector spaces and metric spaces.
- **b.** Read carefully MF ch.3.5. Draw plenty of pictures for Props.3.59 and 3.60 and Cor.3.4 (*A* = interval of real #s)

# Reading assignment 2 - due: Wednesday, September 4:

- **a.** Read carefully B/G ch.3 on logic. It is very brief, but all of it is extremely important.
- **b.** Skim MF ch.4 on logic, just so you have an idea what's in there. Look a little bit more closely at ch.4.5.4 (Quantifiers and Negation). Note that I have marked all of ch.4 as optional, but you will be tested on B/G ch.3!

# Reading assignment 3 - due: Friday, September 6:

**a.** Carefully read MF ch.5 through ch.5.2.4. (A First Look at Direct Images and Preimages of a Function.) You have already encountered much of the material on functions in ch.2.4.

#### written assignments are on the next page.

**General note on written assignments:** Unless expressly stated otherwise, to prove a proposition or theorem you are allowed to make use of everything in the book up to but NOT including the specific item you are asked to prove.

## Written assignment 1:

Let  $(R, \oplus, \odot)$  be an integral domain. Use anything up-to and including MF prop. 3.27 to prove MF prop.3.28: Let  $x \in R$ . If  $x \odot x = x$  then x = 0 or x = 1.

**Hint:** Prove the following: If  $x \odot x = x$  and  $x \neq 0$  then x = 1. Why is that enough?

## Written assignment 2: TOUGH! Get started EARLY!

Let  $(R, \oplus, \odot, P)$  be an ordered integral domain. Use anything up-to and including MF prop. 3.34 to prove MF prop.3.35: The multiplicative unit 1 of *R* belongs to *P*.

**Hint:** This is an **indirect proof!** Part of it: Show that you cannot have  $\ominus 1 \in P$ . **Why** will this help you?

You are **strongly advised** to study the proof of Proposition 3.33 (newly added to MF version 2021-09-01) very thoroughly before working on this problem.