# Math 330 Section 1 - Fall 2024 - Homework 04

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Running total: 18 points

## **Status - Reading Assignments:**

The reading assignments you were asked to complete before the first one of this HW are:

#### MF lecture notes:

ch.1; ch.2.1 - 2.6, ch.3; skim ch.4; ch.5.1 - 5.2.4

B/G (Beck/Geoghegan) Textbook: ch.2.1 – 2.2

B/K lecture notes:

ch.1.1 (Introduction to sets) (optional)

ch.1.2 (Introduction to Functions) but skip ch.1.2.4: Floor and Ceiling Functions (optional)

#### New reading assignments:

### Reading assignment 1 - due Monday, September 9:

- **a.** Read carefully MF ch.5.2.5. Showing that some function is injective and/or surjective will be a major part of many proofs you will encounter later in this course.
- **b.** Read carefully MF ch.5.2.6 5.2.8 (the remainder of ch.5.2). Cartesian products as sets containing families as their elements requires getting used to!

### Reading assignment 2 - due: Wednesday, September 11:

- **a.** Read carefully B/G ch.5 on sets and functions and B/G ch.9.1. You already have encountered the material in MF ch.2 and ch.5.1 5.2.
- **b.** The better students are challenged to take a look at the optional chapter 5.3.
- c. Read extra carefully MF ch.6.1. Proofs by induction will appear on all major exams!
- d. 8Read carefully MF ch.6.2 and 6.3. They are very brief.

### Reading assignment 3 - due: Friday, September 13:

- **a.** Read carefully B/G ch.2.3 on induction. Work through the proofs by induction given there.
- **b.** Carefully read MF ch.6.4 6.6.
- **c.** You are encouraged to look at the optional chapter 6.7 on Bernstein Polynomials. The proofs are very good examples of proofs by induction.

### Written assignments are on the next page.

**General note on written assignments:** Unless expressly stated otherwise, to prove a proposition or theorem you are allowed to make use of everything in the book up to but NOT including the specific item you are asked to prove.

**Written assignment 1:** Use anything before Proposition 3.56 to prove the following part of Proposition 3.56:

Let  $(R, \oplus, \odot, P)$  be an ordered integral domain. Let  $A \subseteq R$ . If A has a minimum then it also has an infimum, and  $\min(A) = \inf(A)$ .

**Written assignment 2:** Use the rules of working with quantifiers to negate the following statement (see B/G ch.3.3). No need at all to understand the meaning of this statement. <sup>1</sup>

 $\forall \alpha > 0 \exists \beta > 0$  such that  $\forall x \in N_{\beta}(z)$  it is true that  $f(x) \in N_{\alpha}(f(z))$ .

<sup>&</sup>lt;sup>1</sup>You will learn later in this course that this is the definition of continuity of a function  $x \mapsto f(x)$  at a point z in the domain of f.