

Math 330 Section 1 - Spring 2026 - Homework 12

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Running total: 39 points

Status - Reading Assignments:

The reading assignments you were asked to complete before the first one of this HW are:

MF lecture notes:

ch.1 – ch.3, skim ch.4, ch.5.1 – ch.12.2 (skip ch.10.3 and ch.11.2.3.)

B/G (Beck/Geoghegan) Textbook:

ch.1 – 7.1, ch.8 – 13.4

Other material (optional):

B/K lecture notes ch.1.1 and ch.1.2, except ch.1.2.4

Stewart Calculus 7ed - ch.1.7: "The Precise Definition of a Limit"

Reading assignments for the Spring Break:

- a. Catch up with your reading. In particular, review Ch.9.3 (Convergence and Continuity in \mathbb{R}) and ch.11.2.2 (Normed Vector Spaces).
- b. Carefully read MF ch.12.3 - ch.12.5. through Example 11.11 (Vector spaces of real-valued functions).
- c. Prepare for the second Midterm!

No written assignments!

Supplementary instructions for reading MF ch.12:

When you read or reread any topics in those chapters then the following is good advice:

- a. MF ch.12.1: Draw as many pictures as possible to get a feeling for the abstract concepts. Use the metric spaces $(\mathbb{R}^2, d_{\|\cdot\|_2})$ and $(\mathcal{B}(X, \mathbb{R}), d_{\|\cdot\|_\infty})$ for this. Do these drawings in particular for
 - open sets and neighborhoods (ch.12.3)
 - convergence, expressed with nhoods (the end of def.12.10 in ch.12.4)
 - metric and topological subspaces (ch.12.7): draw an irregular shaped subset $A \subseteq \mathbb{R}^2$ in two pieces $A = A_1 \uplus A_2$ which do not overlap. Draw some points $x_j \in A$ with ε -nhoods (circles with radius ε about x_j) so that some circles are entirely in A , one with $x_j \in A_1$ which reaches into A° but not into A_2 , and one with $x_j \in A_2$ which reaches both into A° and A_1 . What is $N_\varepsilon^A(x_j)$?
 - Contact points, closed sets and closures (ch.12.8): Draw subsets $B \subseteq \mathbb{R}^2$ with parts of their boundary (periphery) drawn solid to indicate that points there belong to B and other parts drawn dashed to indicate that those boundary points belong to the complement. What is \bar{B} ?
 Draw points “completely inside” B , others “completely outside” B , and others on the solid and dashed parts of the boundary. Which ones can you approximate from within B by sequences? Which ones can you surround by circles that entirely stay within B , i.e., which ones are interior points of B ? Which ones can you surround by circles that entirely stay outside the closure of B , i.e., which ones are entirely within \bar{B}° ? Use those pictures to visualize the definitions in this chapter and thm 12.7 and thm.12.8.
 - Now repeat that exercise with an additional set A which is meant to be a metric subspace of \mathbb{R}^2 .
- b. MF ch.13.2 (Continuity): Draw as many pictures as possible to get a feeling for continuity, especially if you did not take multivariable calculus and are not used to dealing with continuous/differentiable functions of more than one variable. Here is a picture.

Figure 0.1: ε - δ continuity

