Quiz 7 for Math 304-06, 11/6 Your name _____

- (1) (5 points) For vectors $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n$, what does $\mathbf{u} \perp \mathbf{v}$ mean? The answer should be a meaning, not an equation.
- (2) (5 points) For vectors $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n$, what equation corresponds to the statement " $\mathbf{u} \perp \mathbf{v}$ "?

(3) (10 points) Let
$$\mathbf{x} = \begin{bmatrix} 3\\4\\5 \end{bmatrix}$$
 and $\mathbf{y} = \begin{bmatrix} 1\\-1\\0 \end{bmatrix}$.

- (a) How long is the vector \mathbf{x} ?
- (b) Are \mathbf{x} and \mathbf{y} orthogonal?
- (c) Find a vector that is orthogonal to **y**.

(4) (10 points) Suppose we have two bases, $\mathcal{B} = {\mathbf{b}_1, \mathbf{b}_2, \mathbf{b}_3}$ and $\mathcal{C} = {\mathbf{c}_1, \mathbf{c}_2, \mathbf{c}_3}$, for \mathbb{R}^3 and also we have a linear transformation $T : \mathbb{R}^3 \to \mathbb{R}^3$. And suppose

$$[T(\mathbf{b}_1)]_{\mathfrak{C}} = \begin{bmatrix} 1\\2\\3 \end{bmatrix}, \quad [T(\mathbf{b}_2)]_{\mathfrak{C}} = \begin{bmatrix} 1\\0\\-1 \end{bmatrix}, \quad [T(\mathbf{b}_3)]_{\mathfrak{C}} = \begin{bmatrix} 4\\2\\7 \end{bmatrix}.$$

What is the matrix M of T relative to the bases \mathcal{B} and \mathcal{C} ?