

Justify all answers, except where stated.

- (1) [10 points.] What r -combination of what multiset M corresponds to the sequence

$$aaaa|aa||aaa ?$$

What is the value of r ? What is the number of types in M (i.e., k)?

$$M = \text{_____} \quad r = \text{_____} \quad k = \text{_____}$$

- (2) [5 points.] What sequence of a 's and $|$'s corresponds to the solution $(3, 4, 5, 4, 3, 2, 0)$ of the equation $x_1 + x_2 + \cdots + x_7 = 21$?

- (3) [5 points.] What combination from $\{\infty \cdot a_1, \dots, \infty \cdot a_7\}$ corresponds to the solution $(3, 4, 5, 4, 3, 2, 0)$ of the equation $x_1 + x_2 + \cdots + x_7 = 21$?

- (4) [5 points.] What combination from $\{\infty \cdot a_1, \dots, \infty \cdot a_7\}$ corresponds to the solution $(3, 4, 8, 4, 3, 2, -4)$ of the equation $x_1 + x_2 + \cdots + x_7 = 21$?